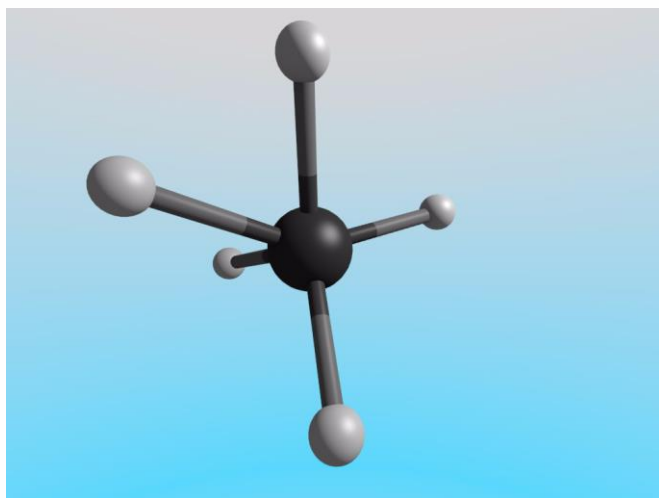


Beyond rotation-vibration separation: Extremely flexible protonated methane

“I anticipate that this enfant terrible will be caught in interstellar space far ahead of its theoretical understanding which will take at least a few more decades.” [1]



Motion in CH₅⁺

- Five protons but four bonds
 - No well-defined, static equilibrium geometry
 - Internal rotations & flips
- ⇒ Rotation and vibration inseparable [2]

~~$$\hat{H}_{\text{full}} = \hat{H}_{\text{rot}} + \hat{H}_{\text{LAV}} + \hat{H}_{\text{SAV}}$$
$$|\psi_{\text{full}}\rangle = |\psi_{\text{rot}}\rangle |\psi_{\text{LAV}}\rangle |\psi_{\text{SAV}}\rangle$$~~

First observation: Free internal rotation angle and axis!

[1] Oka, T.; *Science* **347**, 1313 (2015); Animation: <http://www.theochem.ruhr-uni-bochum.de/go/ch5p.html> (D. Marx)

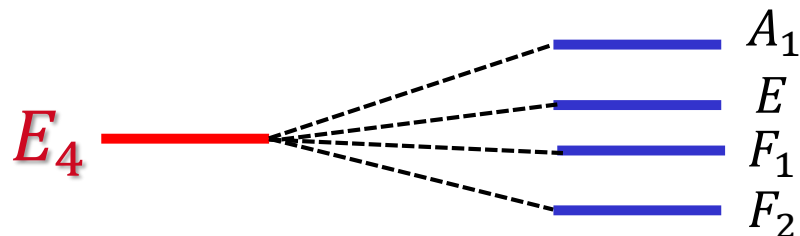
[2] Schmiedt, H., et al. ; *J. Chem. Phys.* **143**, 154302 (2015)

Pedagogical example for better understanding: Rigid methane

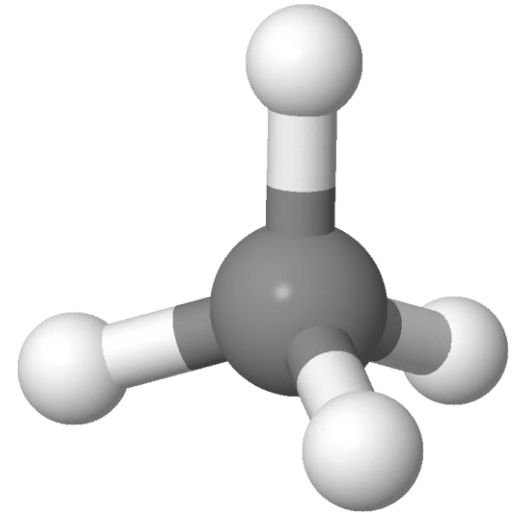
- **Non-vibrating, static methane molecule = rigid spherical top**
- Hamiltonian: $\hat{H} = B(\hat{J}_x^2 + \hat{J}_y^2 + \hat{J}_z^2)$
- Full rotational symmetry: Group $K(\text{mol})$, isomorphic to $SO(3)$
- Irreducible representations $D_J, J = 0, 1, 2, 3, 4, \dots$

$$E_J = B J(J + 1)$$

- **Vibrating, actually existing methane molecule**
- Molecular symmetry group $T_d(M) \subset SO(3)$



Labeled by
irreducible
representations of
 $T_d(M) \subset SO(3)$

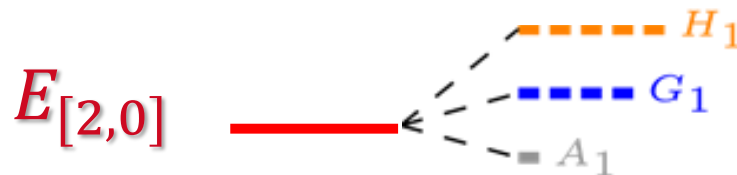


Pedagogical example continued: Protonated methane simplified

- Protonated methane with two “soft” vibrations
- Now five-dimensional rotor [4]: $\hat{H} = \frac{B}{2} \sum_{a < b} \hat{J}_{ab}^2$
- 5D rotational symmetry: Group SO(5)
- Irreducible representations $[n_1, n_2]$, $n_1 \geq n_2 = 0, 1, 2, 3, 4, \dots$

$$E_{[n_1, n_2]} = \frac{B}{2} \{n_1(n_1 + 3) + n_2(n_2 + 1)\}$$

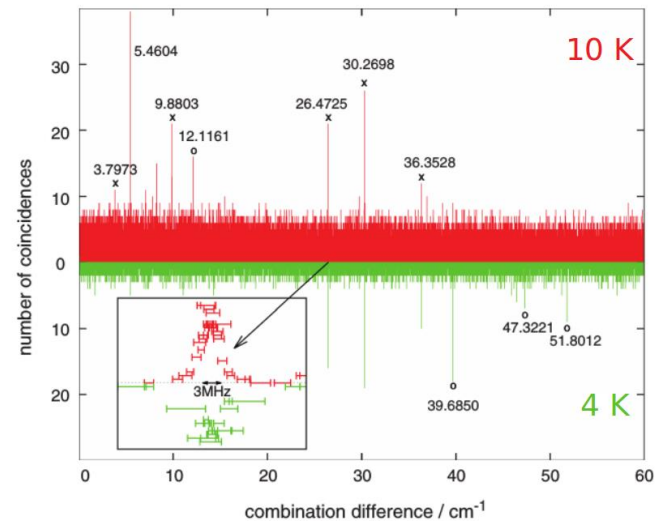
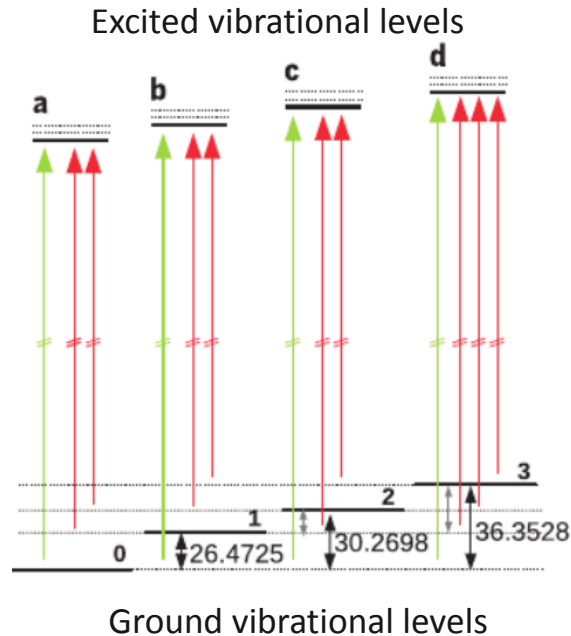
- Fully vibrating, actually existing protonated methane molecule
- Molecular symmetry group $G_{240} \subset SO(5)$



Labeled by
irreducible
representations of
 $G_{240} \subset SO(5)$

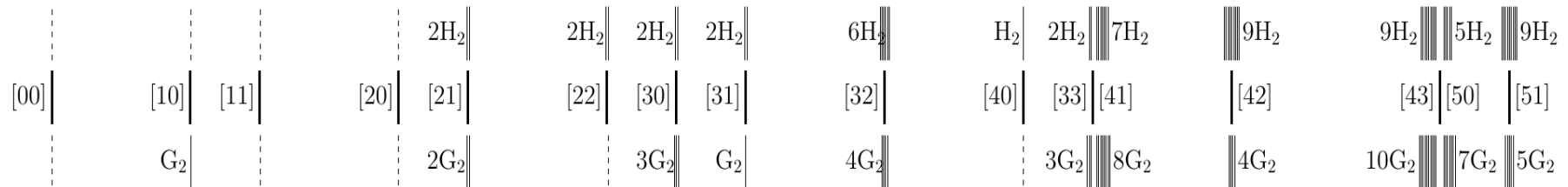
[4] e.g.. Racah, G.; *Phys Rev.* **76**, 1352, (1949)

Rovibrational energies of CH_5^+ from experiment: Combination differences



- Scan rovibrational transitions (infrared)
 - Construct the differences of all transitions (Combination differences = CoDiffs)
 - If two transitions share upper level, this CoDiff occurs regularly (many upper states!)
- ➡ Differences rebuild ground state energy levels [6]

Direct comparison of theory and experiment



Energy

$[cm^{-1}]$

Dashed arrows are experimental GS combination differences

**First assignment of any of these experimental data
consistent in energy and symmetry!**

Dramatis personæ



Hanno Schmiedt
Principal doer

Ponderers (answer phone, pontificate...)



Stephan Schlemmer



Per Jensen

- H. Schmiedt, S. Schlemmer, and P. Jensen: Symmetry of extremely floppy molecules: Molecular states beyond rotation-vibration separation, *J. Chem. Phys.* **143**, 154302/1-8 (2015). DOI: [10.1063/1.4933001](https://doi.org/10.1063/1.4933001)
- H. Schmiedt, P. Jensen, and S. Schlemmer: Collective molecular superrotation: A model for extremely flexible molecules applied to protonated methane, *Phys. Rev. Lett.*, **117**, 223002/1-5 (2016). DOI: [10.1103/PhysRevLett.117.223002](https://doi.org/10.1103/PhysRevLett.117.223002)
- H. Schmiedt, P. Jensen, and S. Schlemmer: Rotation-vibration motion of extremely flexible molecules - The molecular superrotor, *Chem. Phys. Lett.* **672**, 34–46 (2017). DOI: [10.1016/j.cplett.2017.01.045](https://doi.org/10.1016/j.cplett.2017.01.045) "Frontiers article" prepared by invitation.
- H. Schmiedt, P. Jensen, and S. Schlemmer: The role of angular momentum in the superrotor theory for rovibrational motion of extremely flexible molecules, *J. Mol. Spectrosc.*, in press. DOI: [10.1016/j.jms.2017.06.002](https://doi.org/10.1016/j.jms.2017.06.002)



Many thanks for your attention!