

# Vibrational Averaging of the Isotropic Hyperfine Coupling Constants for the Methyl Radical

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# Overview

Theoretical  
Spectroscopy

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Yachmenev<sup>2</sup>,  
and Sergei  
Yurchenko<sup>2</sup>

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# Introduction

## ESR Spectroscopy

### Theoretical Spectroscopy

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### Introduction

### Electronic Structure Calculations

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Comparison to Experiment

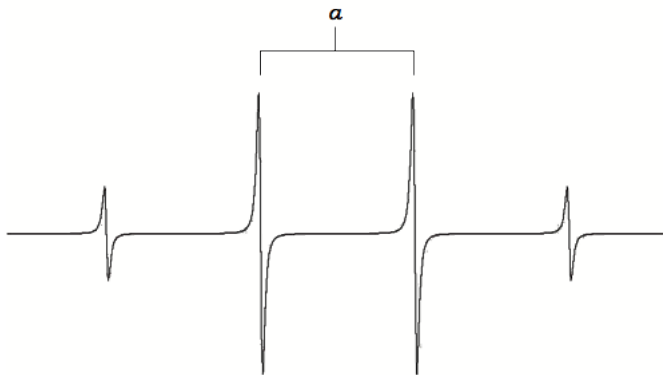
### Nuclear Motion

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HFCC surface  
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- structure of radicals
- detection of radicals
- chemical kinetics
- chemistry, biology, and medicine

# Introduction

Simulated spectrum of  $\text{CH}_3$  radical with hyperfine coupling constant  $a$



**Figure :** Bovet, C.; Barron, A. EPR Spectroscopy: An Overview, OpenStax-CNX Web site. <http://cnx.org/content/m22370/1.3/>, May 23, 2009

Theoretical Spectroscopy

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# Electronic Structure Calculations

## Equilibrium Geometry

Theoretical  
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### Bond distance

- CCSD(T)/aVTZ = 1.0762 Å
- CCSD(T)/aQTZ = 1.0759 Å
- Experiment = 1.079 Å

Half-filled  $2p_z$  orbital

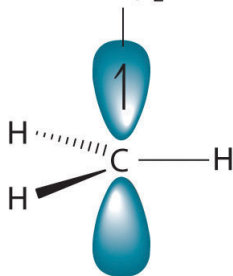


Figure : from Principles of General Chemistry (v.1.0 M) by Bruce A. Averill

# Electronic Structure Calculations

## Theoretical Models and HFCC

Theoretical Spectroscopy

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Effect of

| Method/Basis Set      | $A_{eq}^{iso}, G$ |
|-----------------------|-------------------|
| UB3LYP/ERP-III        | 28.2              |
| CISD/DZ               | 25.7              |
| CCSD(T)/Chipman       | 28.5              |
| B3LYP/Huz-IVu4s       | 30.1              |
| UB3LYP/EPR-III        | 28.6              |
| UB2PLYP/EPR-III       | 30.0              |
| OO-RI-MP2/EPR-III     | 30.0              |
| OO-SCS-RI-MP2/EPR-III | 22.0              |
| CCSD(T)/EPR-III       | 24.7              |

**Table :**  $^{13}C$  isotropic HFCC in  $CH_3$  (Table data from Chen X, Rinkevicius Z, Ruud K, Ågren H., *J. Chem. Phys.* 2013, 138, 054310. See this paper for original references.)

# Electronic Structure Calculations

## Comparison to Experiment

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| OO-SCS-RI-MP2/EPR-III | 22.0              |
| CCSD(T)/EPR-III       | 24.7              |
| <b>Experiment</b>     | <b>38.3</b>       |

**Table :**  $^{13}\text{C}$  isotropic HFCC in  $\text{CH}_3$  (Table data from Chen X, Rinkevicius Z, Ruud K, Ågren H., *J. Chem. Phys.* 2013, 138, 054310. See this paper for original references.)

# Nuclear Motion

## Thermal Averaging

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### Theory

- $\langle P \rangle_T = \frac{1}{Q} \sum_i g_i \exp\left(-\frac{E_{rv}^{(i)}}{kT}\right) \langle P \rangle_i$

- $Q = \sum_i g_i \exp\left(-\frac{E_{rv}^{(i)}}{kT}\right)$

- $\langle P \rangle_i = \langle \Phi_{rv}^{(i)} | P | \Phi_{rv}^{(i)} \rangle$

where ..

P = operator

T = absolute temperature

Q = partition function

$g_i$  = degeneracy



# Nuclear Motion

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- $\langle P \rangle_i = \langle \Phi_{rv}^{(i)} | P | \Phi_{rv}^{(i)} \rangle$

where ..

P = operator

T = absolute temperature

Q = partition function

$g_i$  = degeneracy

$E_{rv}^{(i)}$  = eigenvalues

$\Phi_{rv}^{(i)}$  = eigenvectors

### Theoretical ROVibrational Energies (TROVE): A robust numerical approach to the calculation of rovibrational energies for polyatomic molecules

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### Thermal averaging of the indirect nuclear spin-spin coupling constants of ammonia: The importance of the large amplitude inversion mode

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# Nuclear Motion

## Potential Energy and HFCC Surfaces

Theoretical  
Spectroscopy

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- 2625 unique symmetry points near equilibrium geometry
- UHF-CCSD(T)/aug-cc-pVTZ for Potential Energy Surface
- UHF-CCSD(T)/EPR-III for HFCC surface
- Least squares fitting

# Nuclear Motion

## Vibrational Contribution to HFCC

### Theoretical Spectroscopy

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Effect of

| Method/Basis Set   | $A_{eq}^{iso}$<br>(G) | $A_{vib}^{iso}$<br>(G) | $\Delta A_{vib}^{iso}$<br>(G) | Temp.<br>(K) |
|--------------------|-----------------------|------------------------|-------------------------------|--------------|
| B3LYP/Huz-IIIsu3   | 29.9                  | 42.2                   | 12.3 (41%)                    | 0            |
| P(CI)/DZ           | 22.2                  | 35.1                   | 12.9 (58%)                    | 96           |
| MCSCF/cc-pVTZus2st | 27.7                  | 37.3                   | 9.6 (35%)                     | 0            |
| CCSD(T)/EPR-III    | 24.7                  | 36.49                  | 11.8 (48%)                    | 0            |
| CCSD(T)/EPR-III    | 24.7                  | 36.51                  | 11.8 (48%)                    | 96           |
| Experiment         | –                     | 38.3                   | –                             | 96           |

**Table :** <sup>13</sup>C isotropic HFCC in CH<sub>3</sub> (Table data from Chen X, Rinkevicius Z, Ruud K, Ågren H., *J. Chem. Phys.* 2013, 138, 054310. See this paper for original references.) Our work is in blue color

# Nuclear Motion

## Effect of Temperature

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| CCSD(T)/EPR-III    | 24.7                  | 36.51                  | 11.8 (48%)                    | 96           |
| Experiment         | –                     | 38.3                   | –                             | 96           |
| CCSD(T)/EPR-III    | 24.7                  | 37.53                  | 12.8 (52%)                    | 300          |

Table : <sup>13</sup>C isotropic HFCC in CH<sub>3</sub> (Table data from Chen X, Rinkevicius Z, Ruud K, Ågren H., *J. Chem. Phys.* 2013, 138, 054310. See this paper for original references.) Our work is in blue color

# Summary and Conclusions

## Theoretical Spectroscopy

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### Vibrational Contribution to HFCC

### Effect of

- Vibrational effects cannot be ignored in the case of  $^{13}\text{C}$  isotropic HFCC for  $\text{CH}_3$
- Compared to other averaging methods, our averaging included the rotational motion and coupling between vibrational modes
- With temperature effects, the ro-vibrational contribution will exceed the electronic contribution

# Acknowledgment

## Theoretical Spectroscopy

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- Andrey Yachmenev (UCL) for many helpful discussions
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Forschungsgemeinschaft