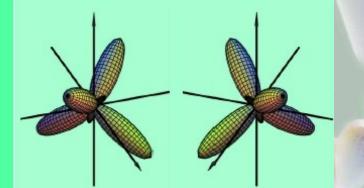


INSTITUTE OF PHYSICS SERIES IN CHEMICAL PHYSICS



## FUNDAMENTALS OF MOLECULAR Symmetry

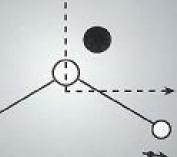
The prequel to

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MOLECULAR SYMMETRY AND SPECTROSCOPY SECOND EDITION



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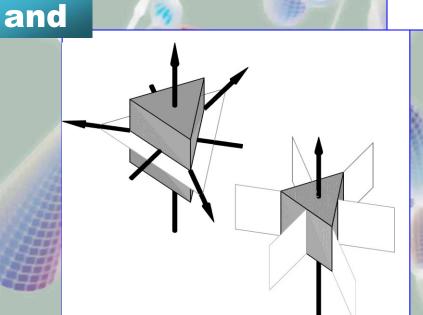
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how is it understood?
how and when is it used?

Includes a concise description of molecular spectroscopy and quantum mechanics

> For undergraduate and research students in molecular science

A balanced account of

## MOLECULAR SYMMETRY (MS) GROUPS



**POINT GROUPS** 

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