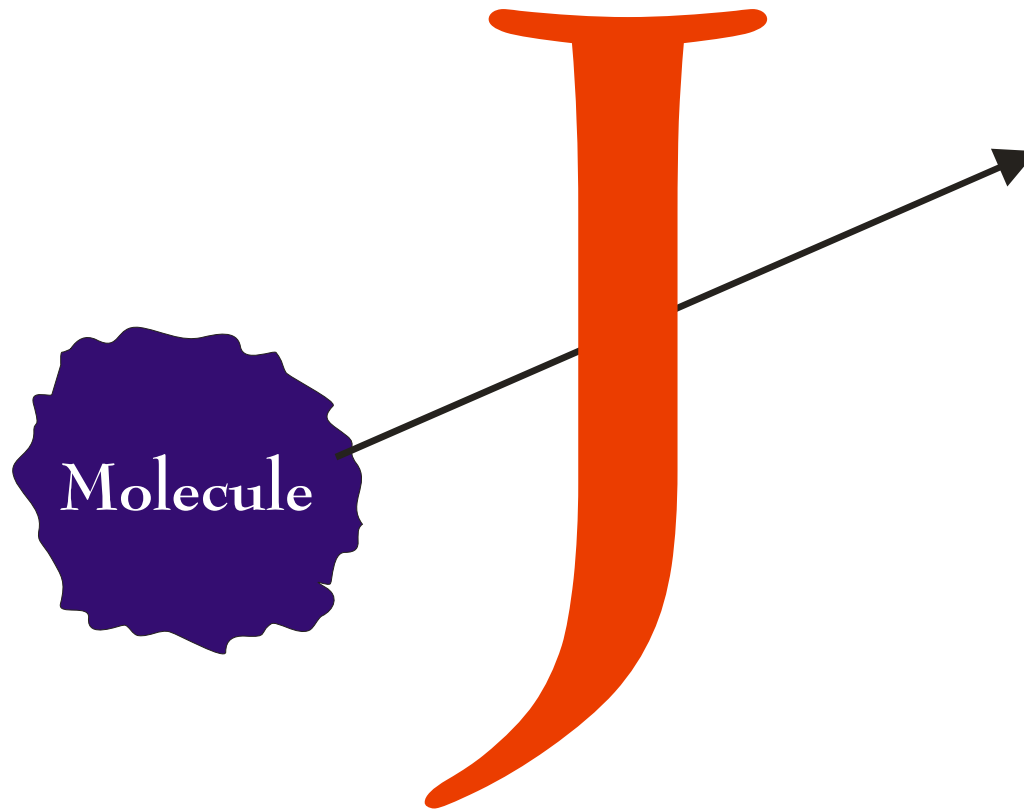
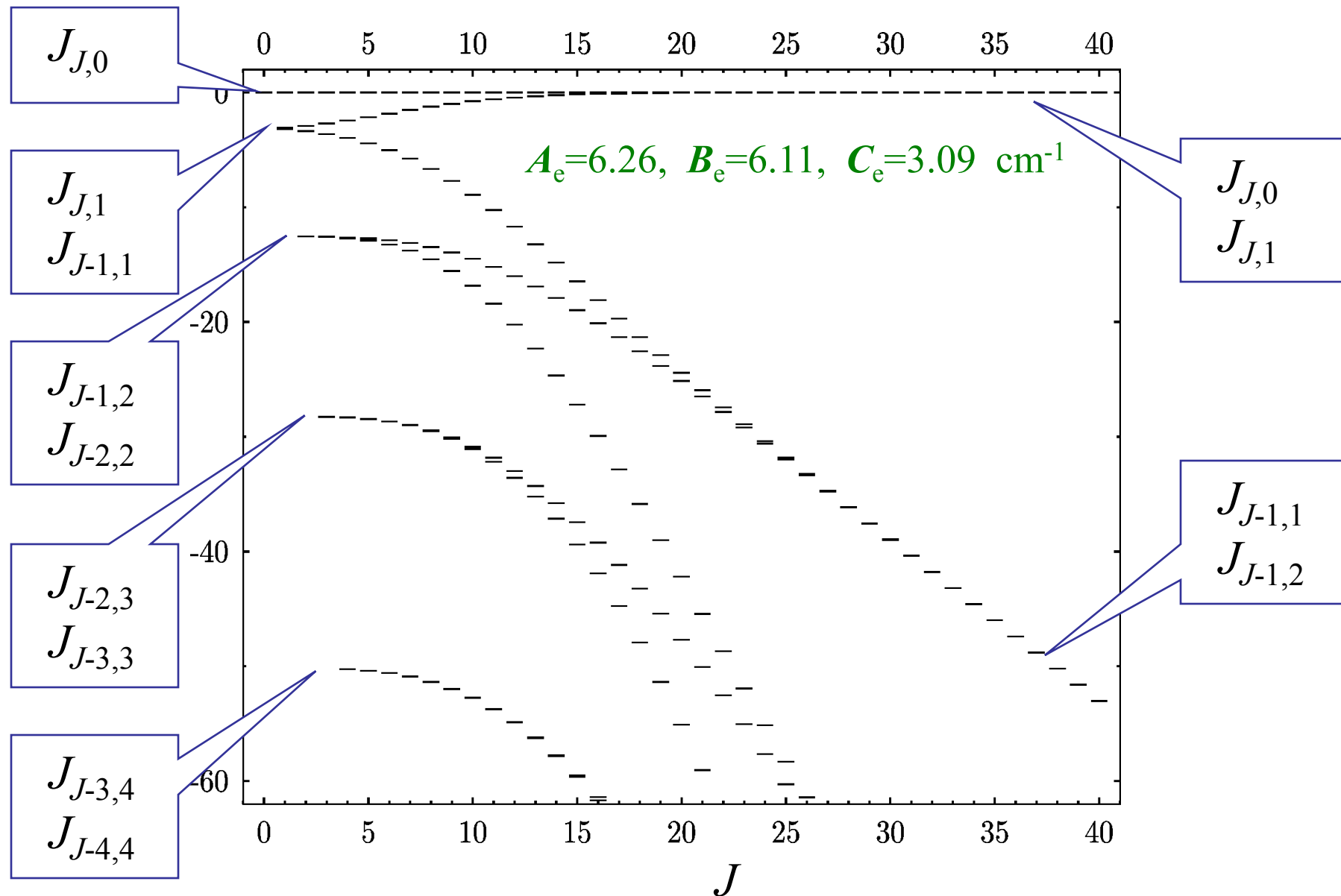


Molecules in highly excited rotational states

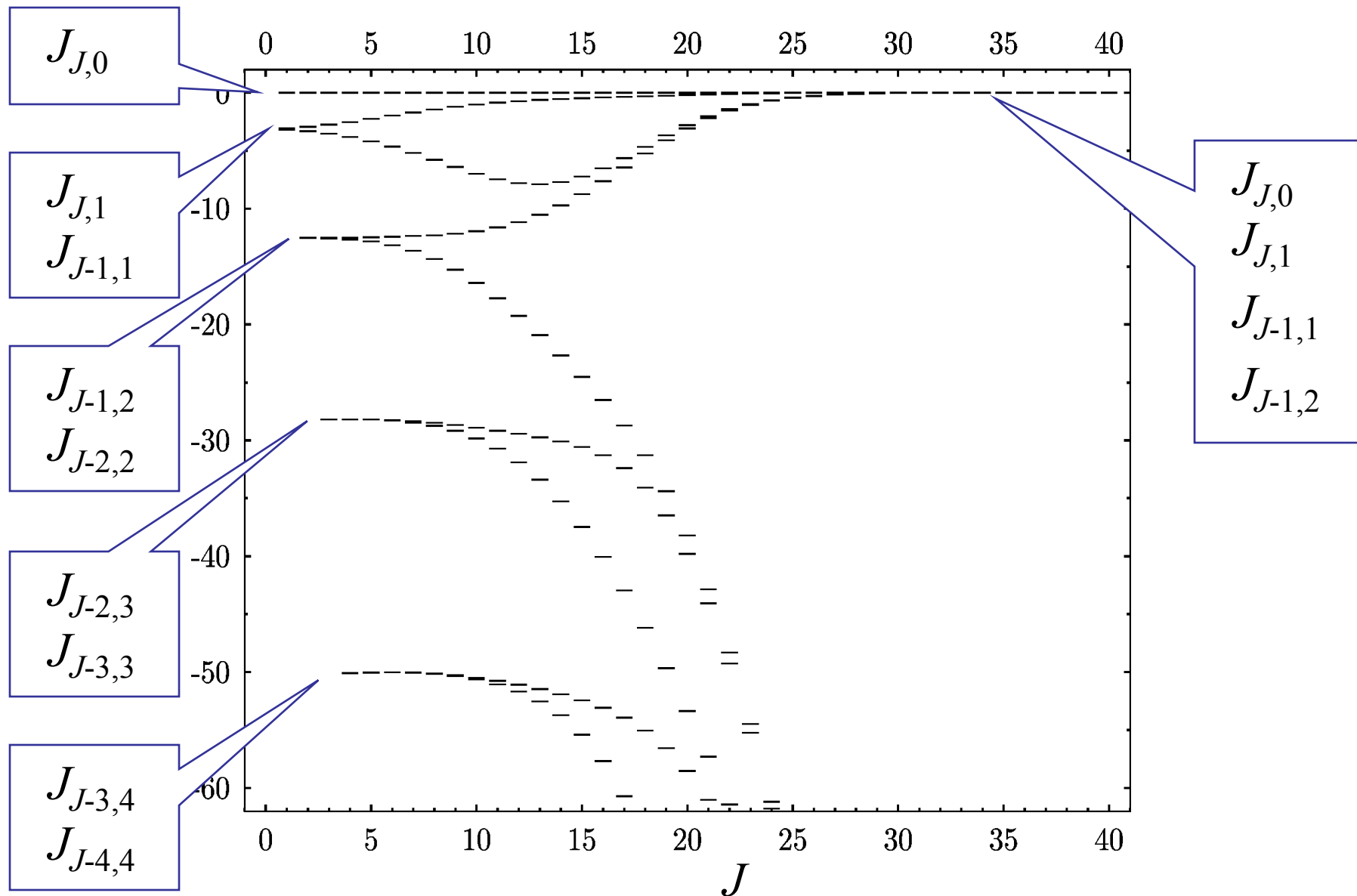


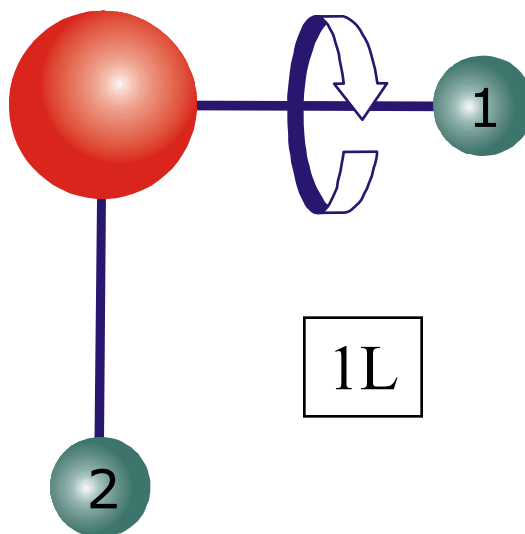
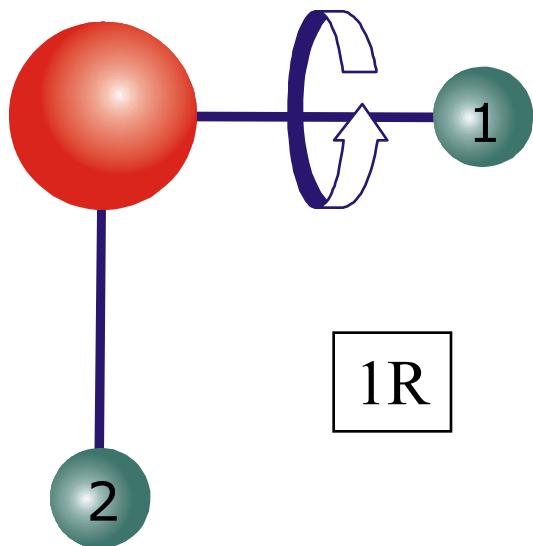
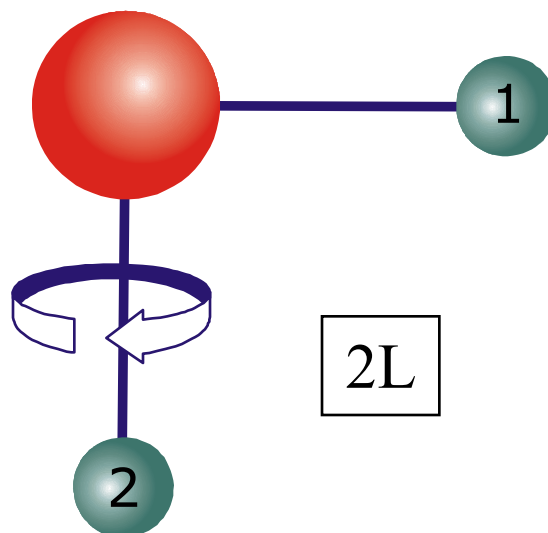
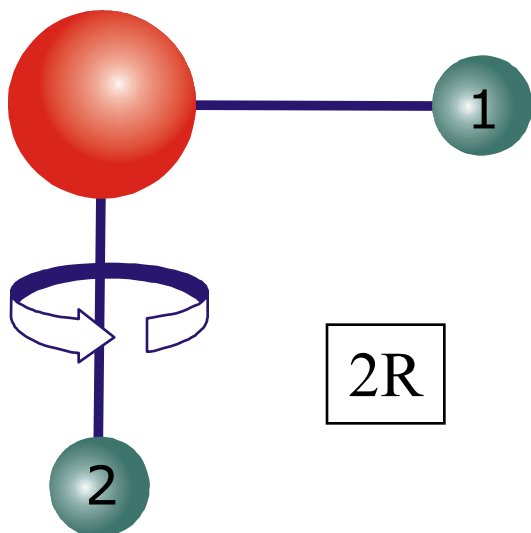
$$J \sim 100$$

H₂Te Rigid Rotor Energy Levels [$E(J_{KaKc})-E(J_{J0})$]



Actual H₂Te Energy Levels [$E(J_{KaKc})-E(J_{J0})$]



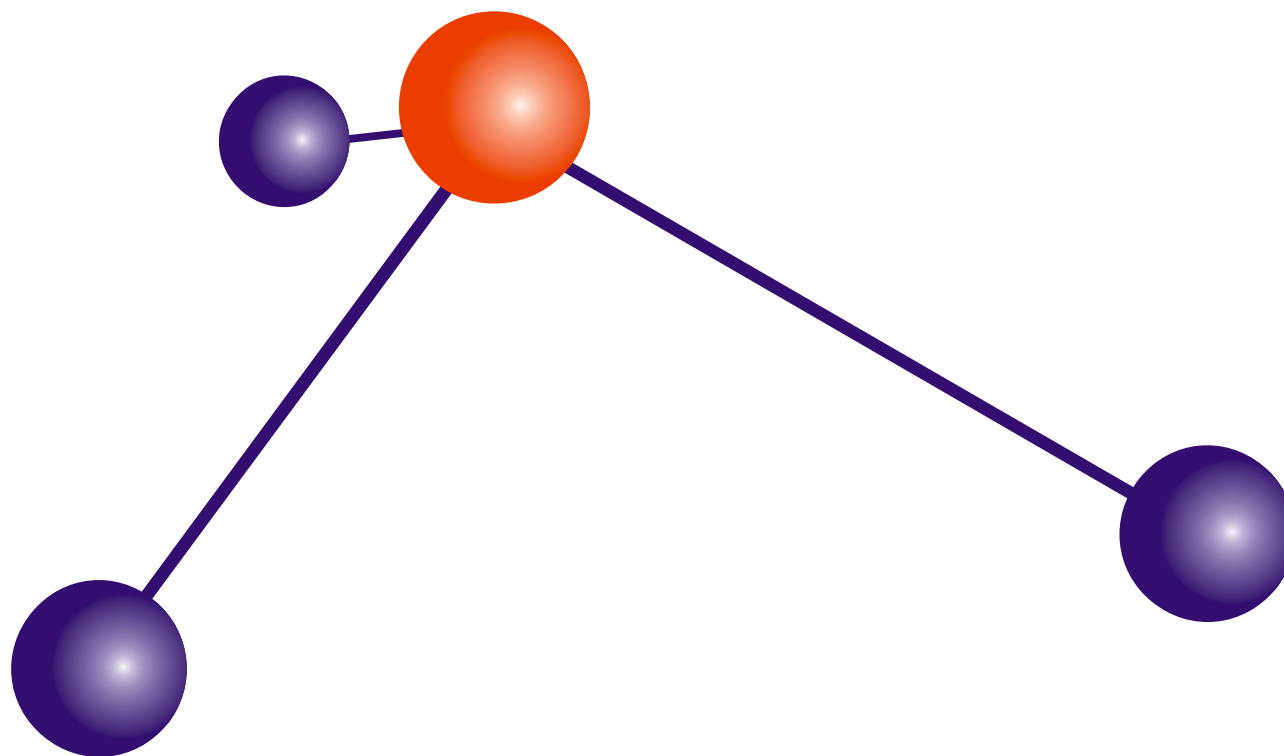


$$\left. \begin{array}{l} J_{J,0} \\ J_{J,1} \\ J_{J-1,1} \\ J_{J-1,2} \end{array} \right\} \equiv \equiv \equiv$$

$$\Gamma_{\text{Cluster}} = A_1 \oplus A_2 \oplus B_1 \oplus B_2 \quad \text{in } C_{2v}(\mathbf{M})$$

Rotational Energy Level Clusters

1972	Dorney and Watson	CH ₄	8-fold and 6-fold clusters
1978	Zhilinskii and Pavlichenkov	H ₂ O	4-fold clusters (E_{rb})
1978	Harter and Patterson		Rotational energy surfaces and clusters
1991	Lehmann		Local mode theory and clusters
1992	Kozin et al	H ₂ Se	4-fold clusters observed
1993	Kozin and Jensen	H ₂ Se	4-fold cluster theory (E_{rbs})
1994	Jensen and Bunker	H ₂ X	4-fold cluster symmetry
1996	Kozin et al	H ₂ Te	4-fold clusters (exp and theory)
1997	Jensen et al		Review paper on 4-fold clusters
2000	Jensen		Review paper on LMT and clusters [<i>Mol. Phys.</i> 98 , 1253-1285 (2000)]



**Are there similar effects for
 XH_3 molecules – say PH_3 ?**

Programs: XY3 and TROVE

(Theoretical Rotation-Vibration Energies)

XY3: Rotation-vibration energies for pyramidal, ammonia-type molecule in isolated electronic state, calculated variationally.

[1] H. Lin *et al.*, *J. Chem. Phys.* **117**, 11265 (2002)

[2] S.N. Yurchenko *et al.*, *Mol. Phys.* **103**, 359 (2005) and references given there.

TROVE: Rotation-vibration energies for any molecule in isolated electronic state, calculated variationally.

[3] S.N. Yurchenko, W. Thiel, and P. Jensen, *J. Mol. Spectrosc.* **245**, 126 (2007)

Variational rotation-vibration calculations for PH₃

$$J \leq 80$$

Vibrational basis set:

$$2(\nu_1 + \nu_2 + \nu_3) + \nu_{inv} + V_{bend} \leq 6$$

Potential energy surface:

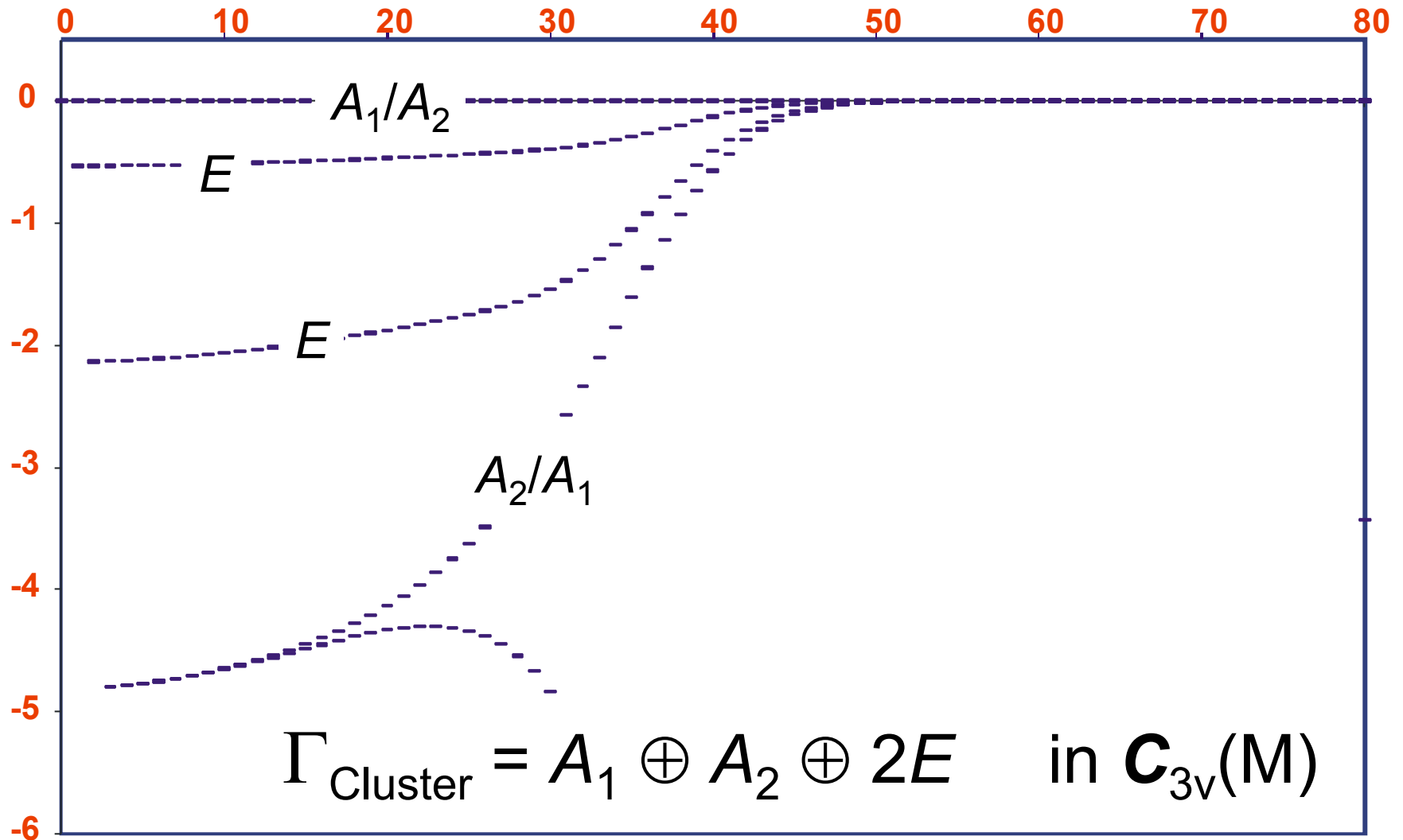
cc-pwCVTZ [1]

refined by fitting to experimental
vibrational term values [2]

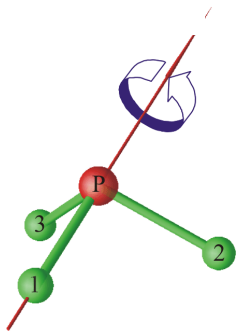
[1] D. Wang, Q. Shi, and Q.-S. Zhu, *J. Chem. Phys.*, **112**, 9624 (2000)

[2] S.N. Yurchenko *et al.*, *Chem. Phys.* **290**, 59 (2003)

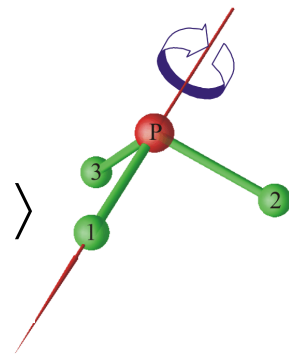
Yes, there are six-fold clusters!



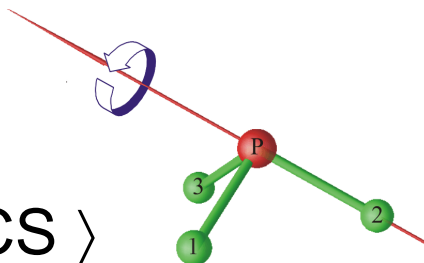
$$|1 \text{ PCS} \rangle = E |1 \text{ PCS} \rangle$$



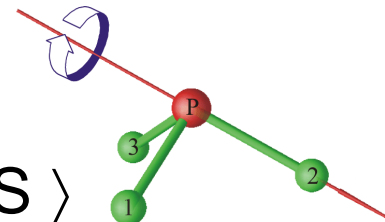
$$|4 \text{ PCS} \rangle = (23)^* |1 \text{ PCS} \rangle$$



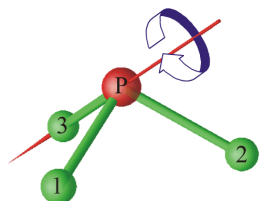
$$|2 \text{ PCS} \rangle = (123) |1 \text{ PCS} \rangle$$



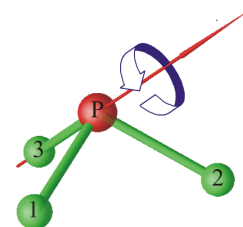
$$|5 \text{ PCS} \rangle = (12)^* |1 \text{ PCS} \rangle$$



$$|3 \text{ PCS} \rangle = (132) |1 \text{ PCS} \rangle$$

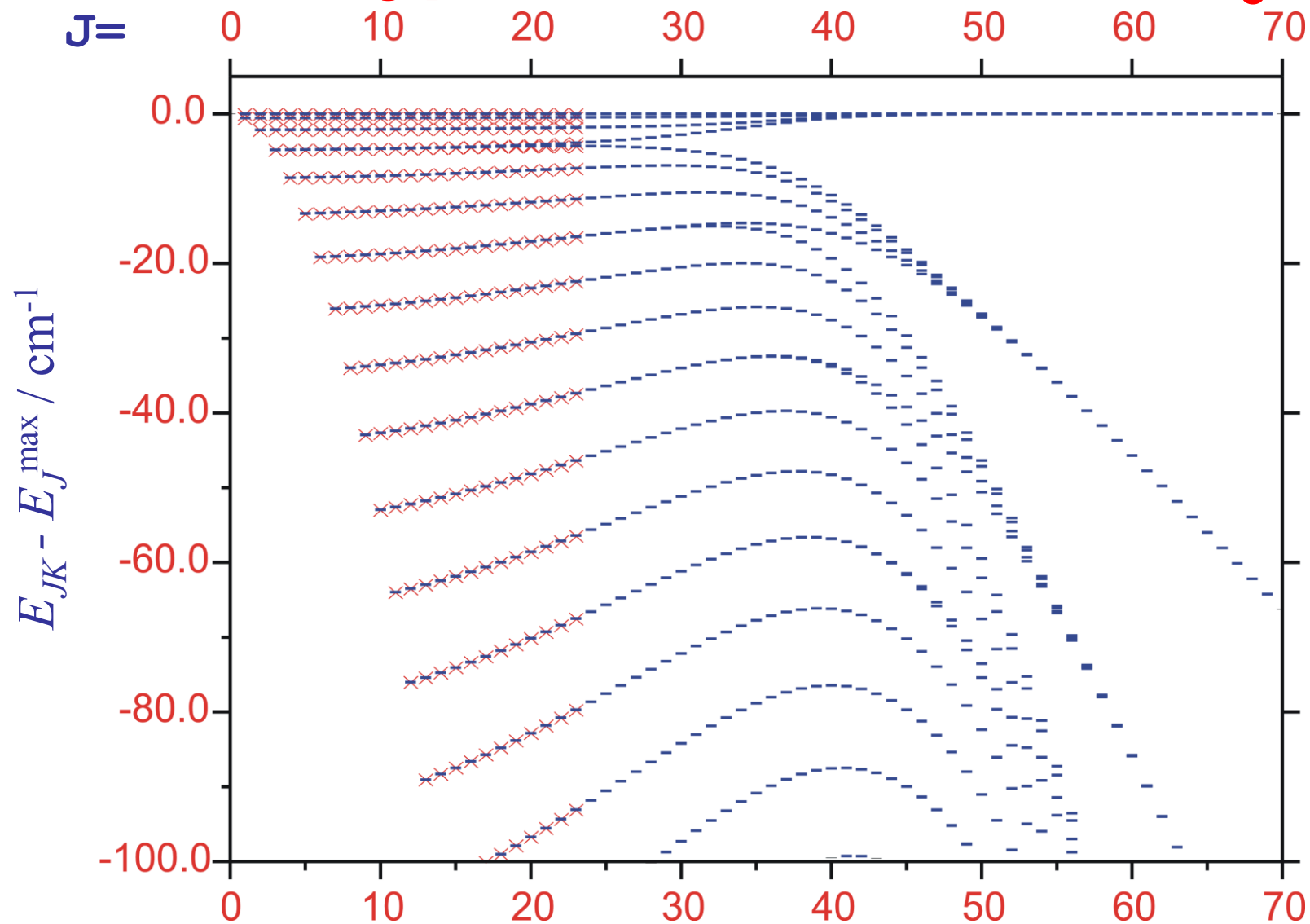


$$|6 \text{ PCS} \rangle = (13)^* |1 \text{ PCS} \rangle$$



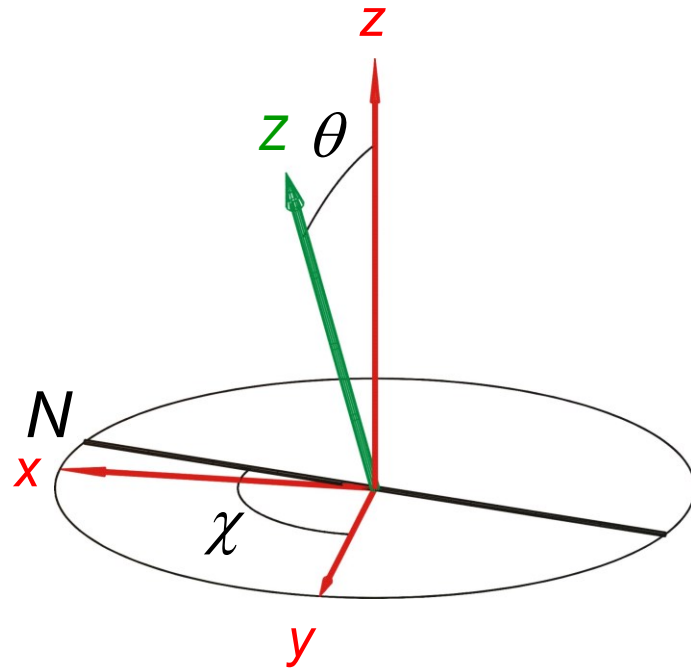
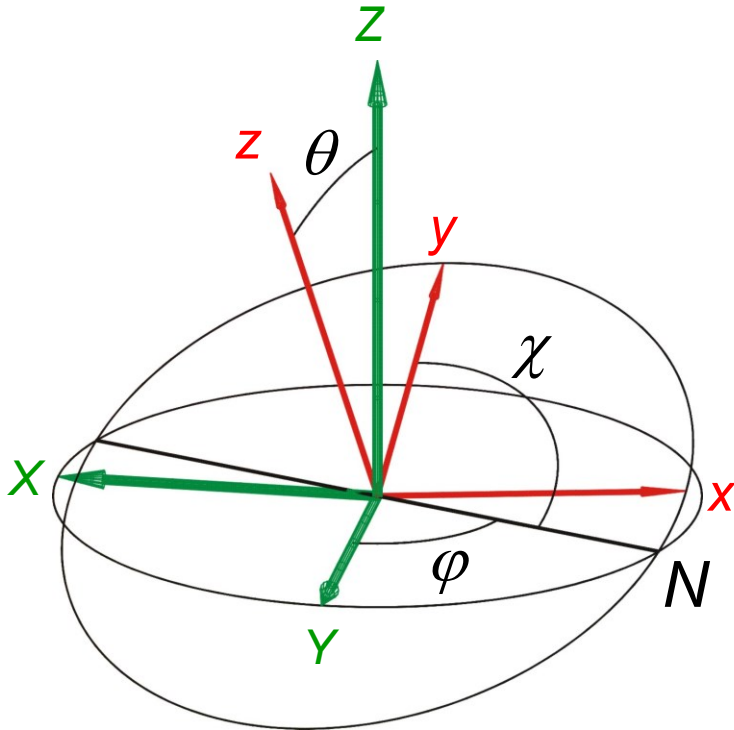
$$\Gamma_{\text{Cluster}} = A_1 \oplus A_2 \oplus 2E \quad \text{in } \mathbf{C}_{3v}(\text{M})$$

Watson-type Hamiltonian for PH₃



Rotational coordinates

xyz is molecule-fixed; XYZ is space-fixed



- (θ, φ, χ) define orientation of molecule (xyz) relative to laboratory (XYZ).
- (θ, χ) define orientation of Z axis relative to molecule (xyz).

For a rovibronic eigenstate Φ_i

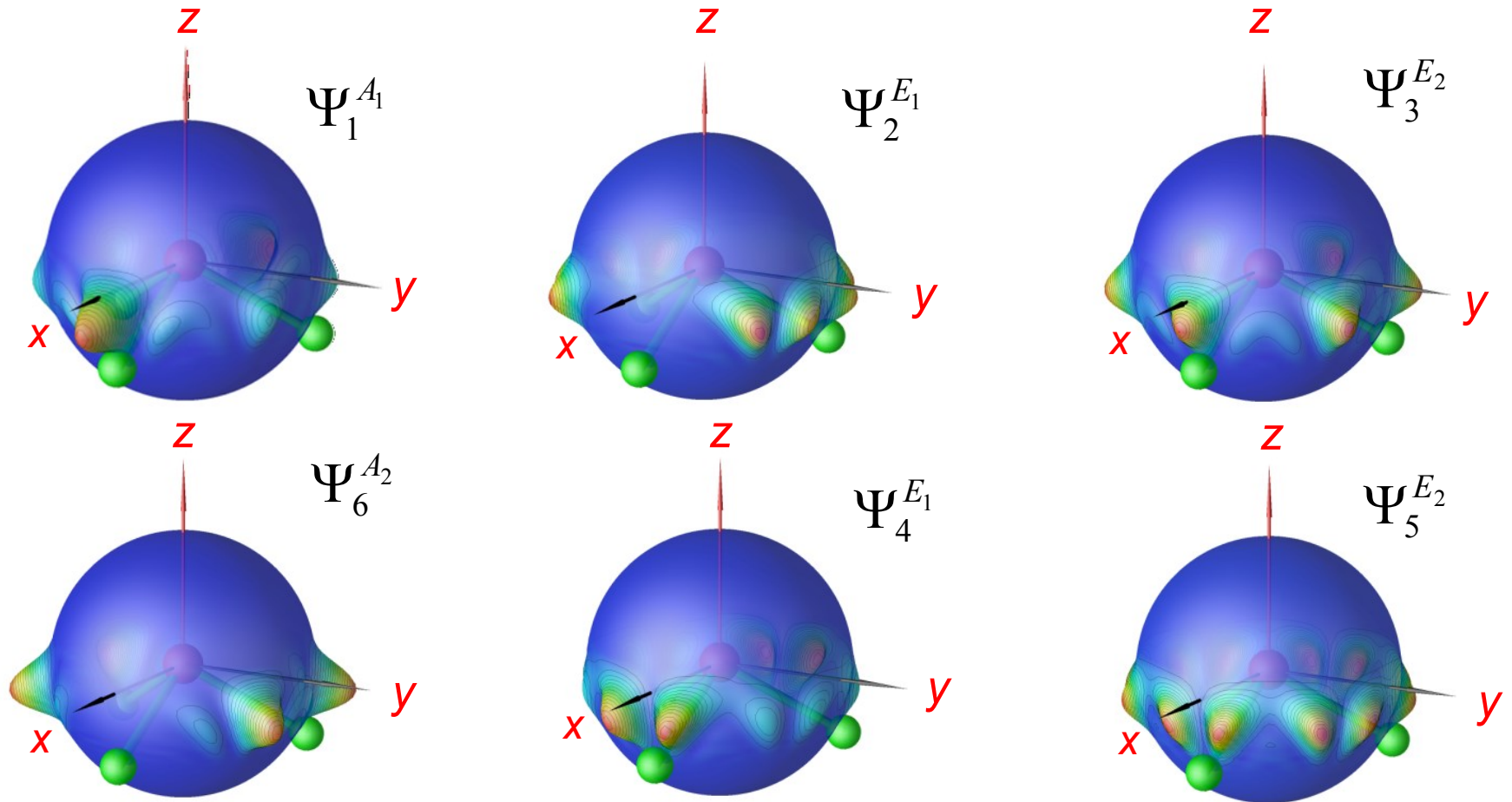
$$F_{J,m}(\theta, \chi) = \int (\Phi_i)^* \Phi_i \sin \theta dV$$



Integration over all vibronic coordinates and φ

is the probability distribution for the orientation of the **Z axis** relative to the molecule.

$$F_{J,m}(\theta, \chi)$$



**“Top cluster states” for $J = m = 40$,
vibrational ground state of PH_3**

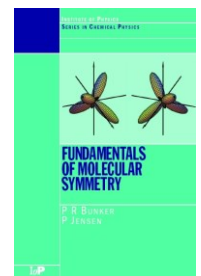
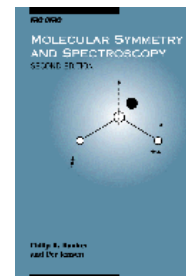
Primitive cluster states $|j \text{ PCS} \rangle$

First symmetrize, e.g.

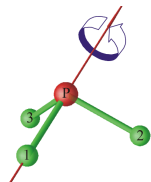
$$\Psi_1^{A_1} = \frac{1}{\sqrt{6}} \left(|1 \text{ PCS} \rangle + |2 \text{ PCS} \rangle + |3 \text{ PCS} \rangle + |4 \text{ PCS} \rangle + |5 \text{ PCS} \rangle + |6 \text{ PCS} \rangle \right)$$

$$\Psi_6^{A_2} = \frac{1}{\sqrt{6}} \left(|1 \text{ PCS} \rangle + |2 \text{ PCS} \rangle + |3 \text{ PCS} \rangle - |4 \text{ PCS} \rangle - |5 \text{ PCS} \rangle - |6 \text{ PCS} \rangle \right)$$

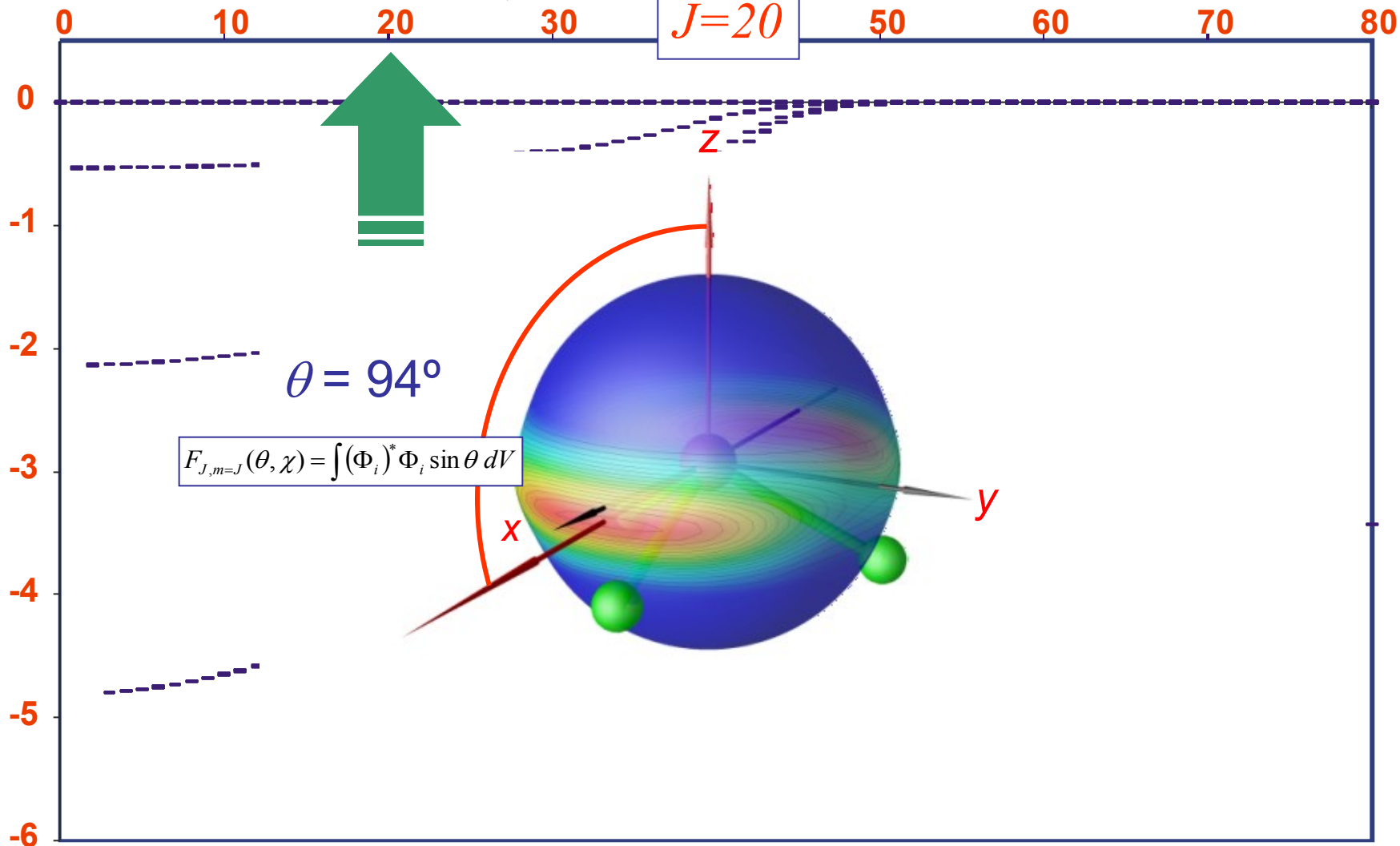
with similar expressions for the E functions....



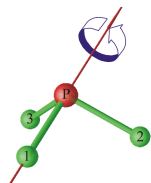
$|1 \text{ PCS} \rangle$



$J=20$

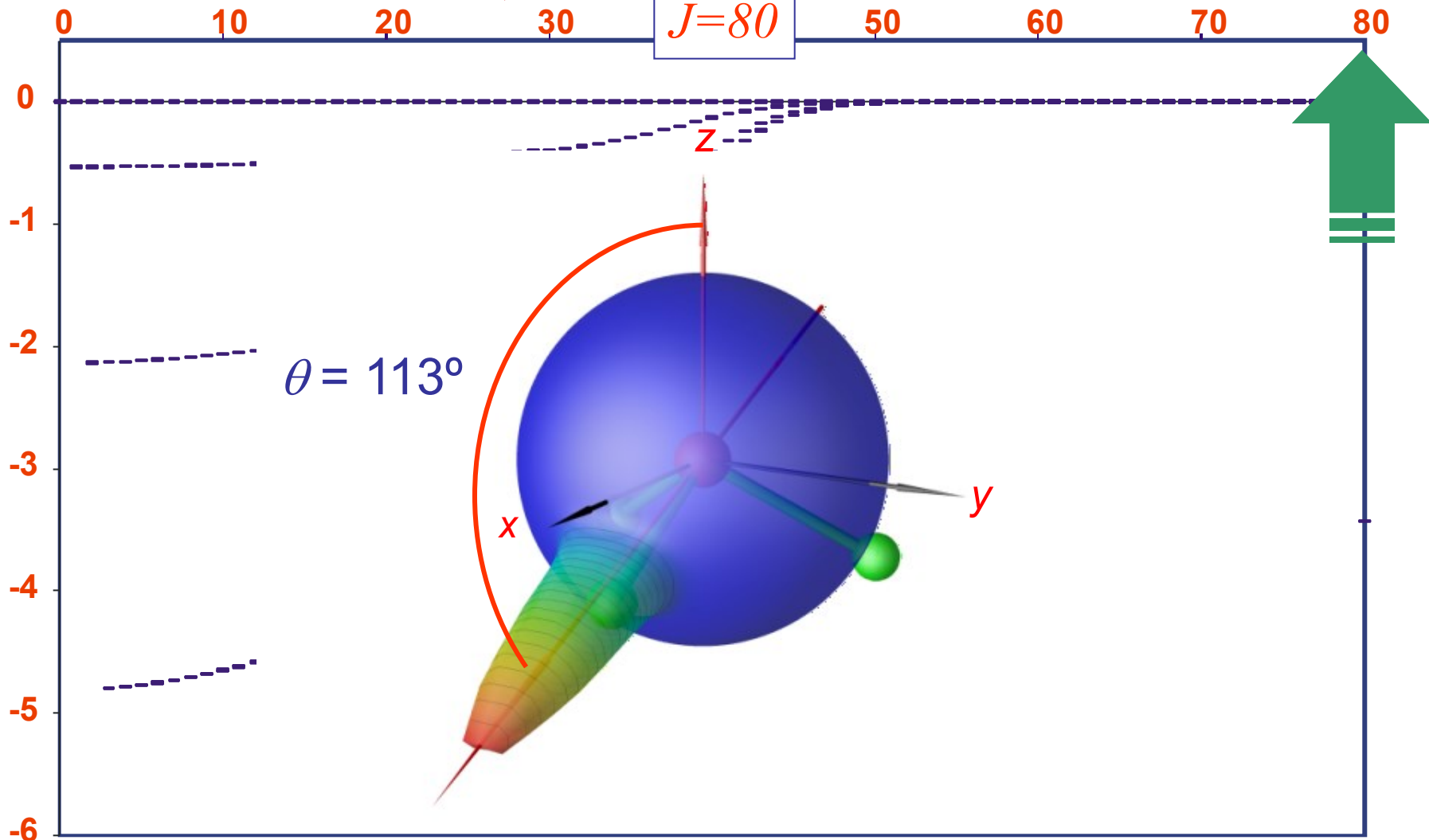


$|1 \text{ PCS} \rangle$

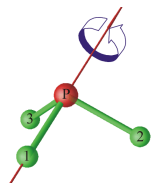


$$\theta_{\text{eq}} = 123^\circ$$

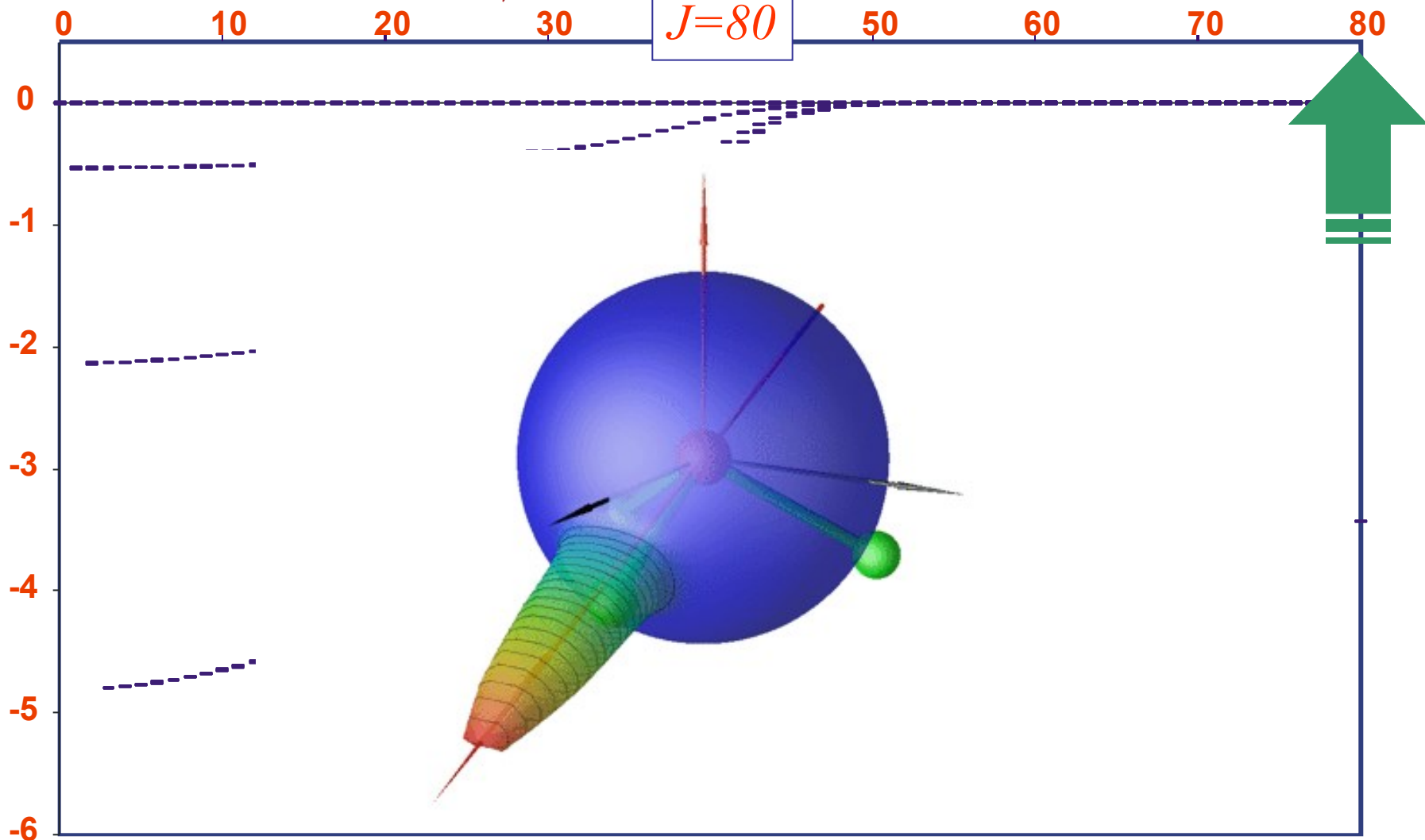
$J=80$



$|1 \text{ PCS} \rangle$



$J=80$

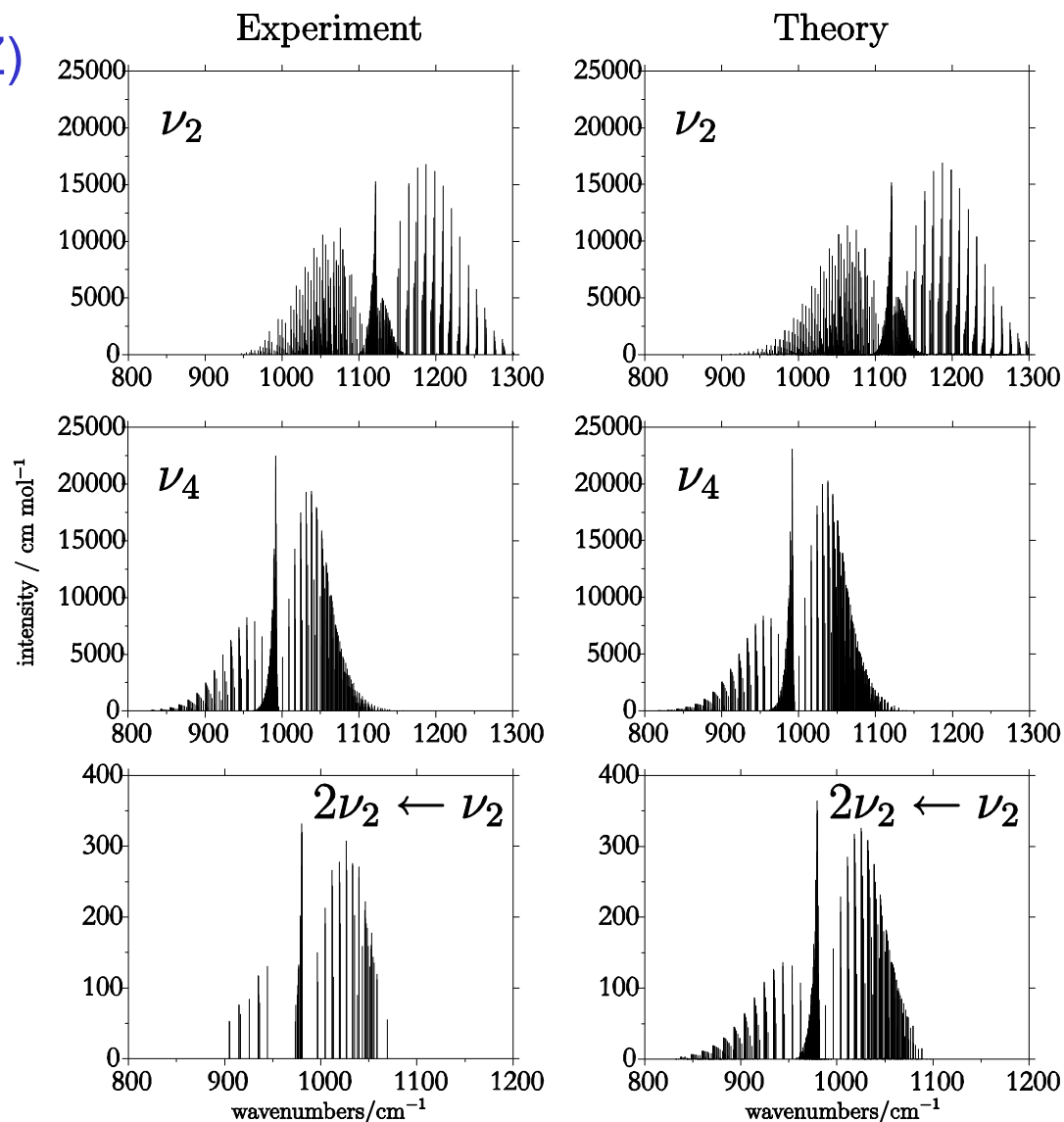


PH₃ intensity calculations

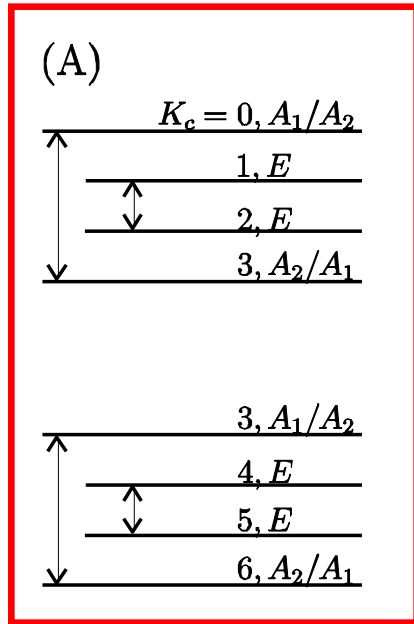
Ab initio (CCSD(T)/aug-cc-pVTZ)
dipole moment surfaces

Rotation-vibration
wavefunctions from
the variational
calculation

Experimental data
from L. R. Brown,
R. L. Sams, I. Kleiner,
C. Cottaz, and L. Sagui,
J. Mol. Spectrosc. **215**,
178-203 (2002)

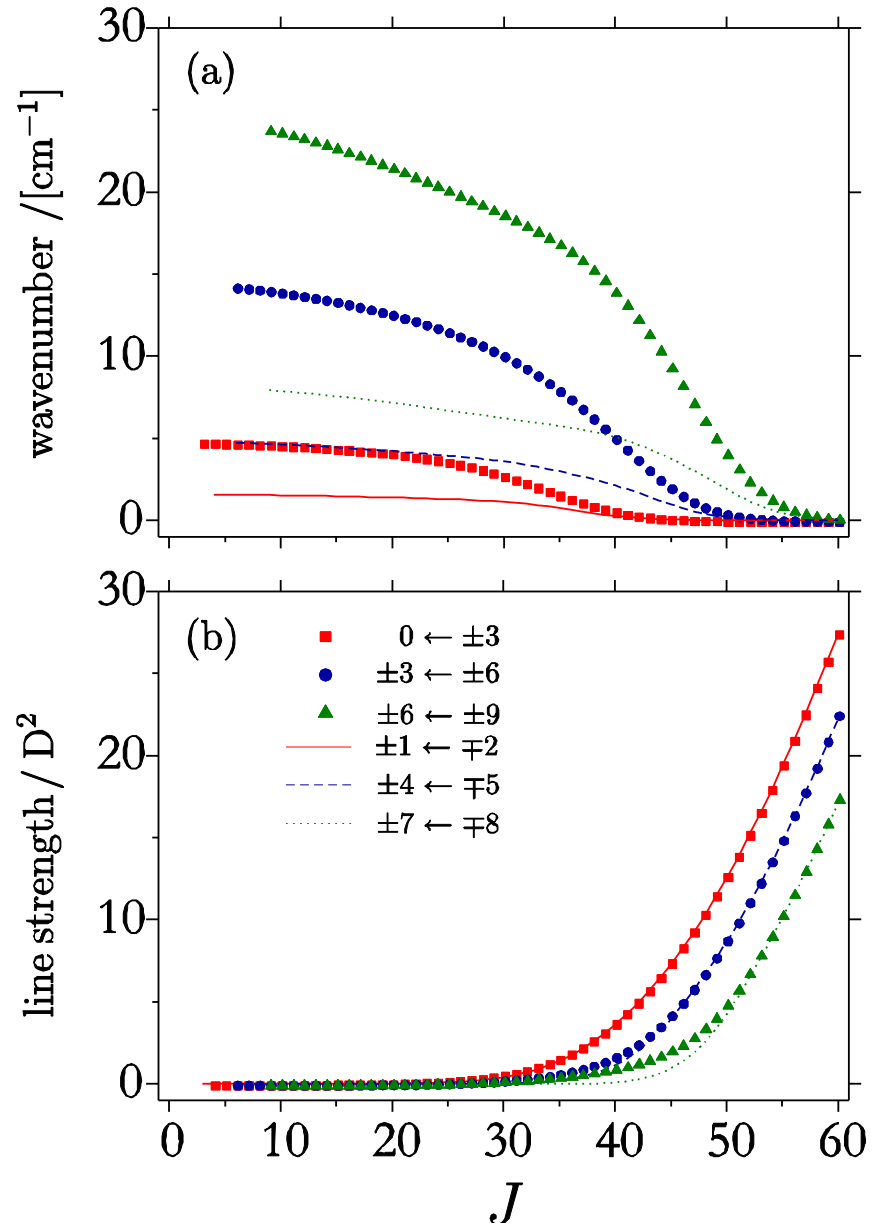


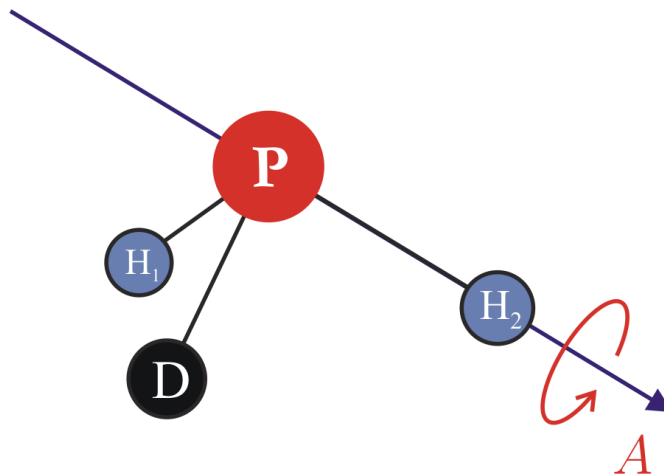
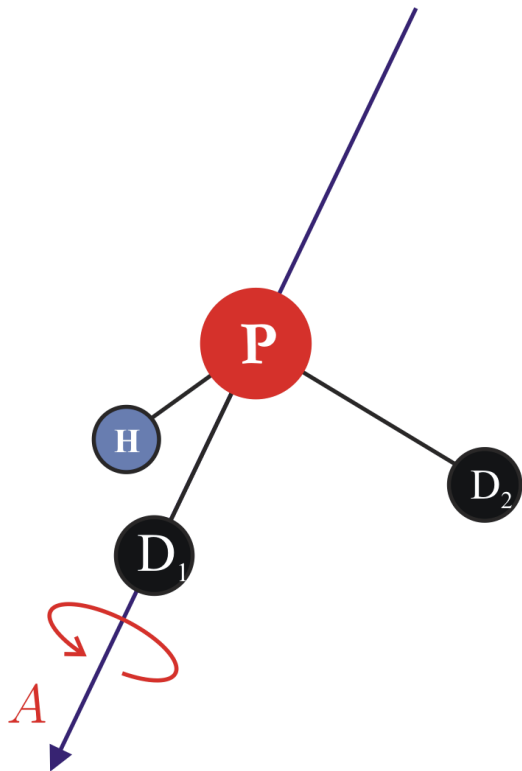
PH₃ cluster transitions



Large line strengths
at high J

Can the lower states
be populated somehow?

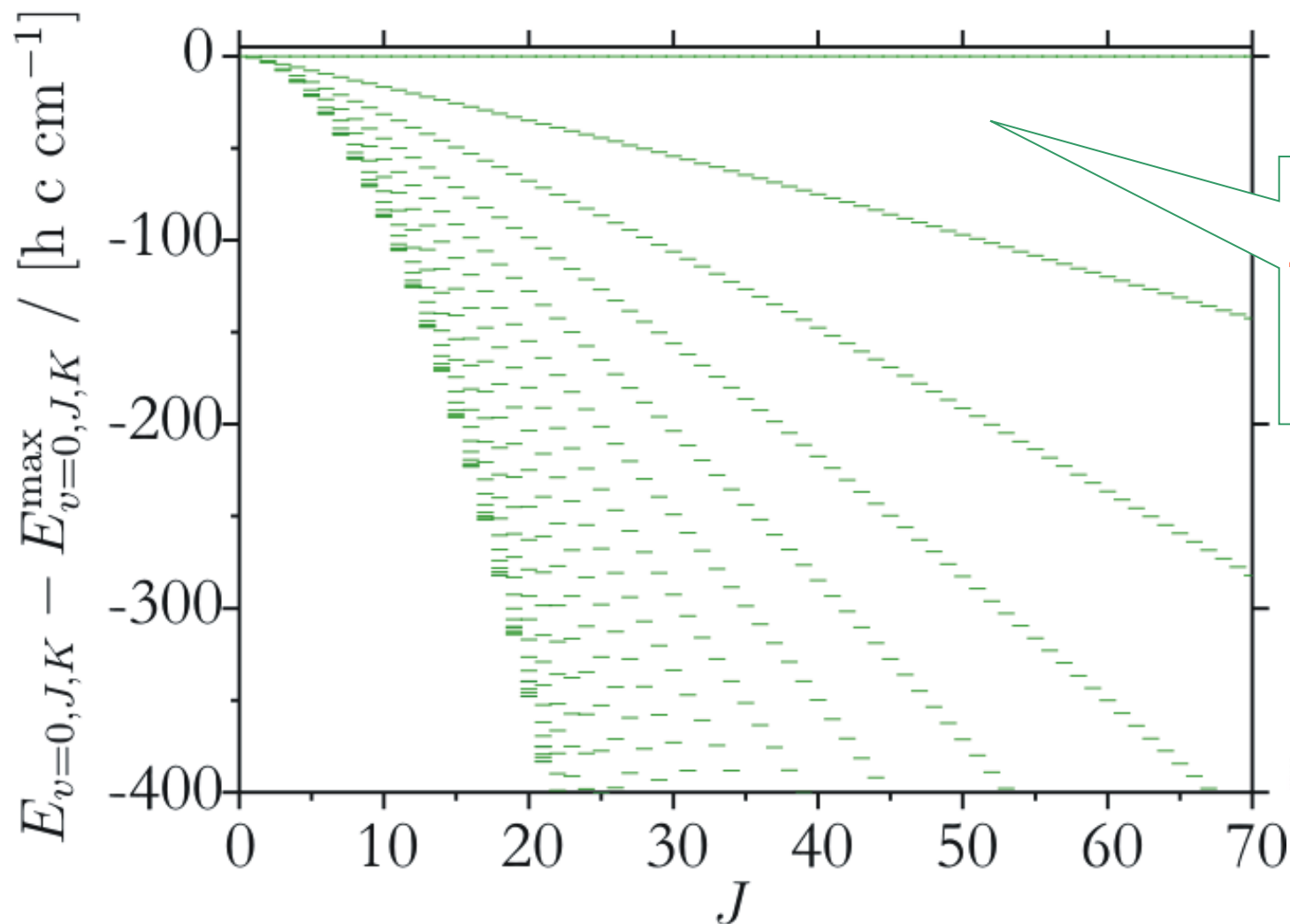




?

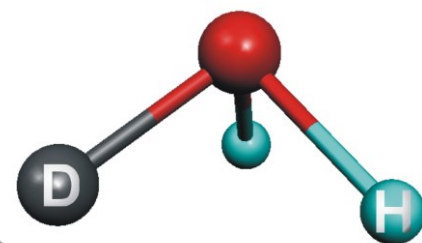
Also similar effects for
 XHD_2 or XH_2D molecules,
 say PHD_2 or PH_2D ?

PH₂D rotational energies: TROVE calculations

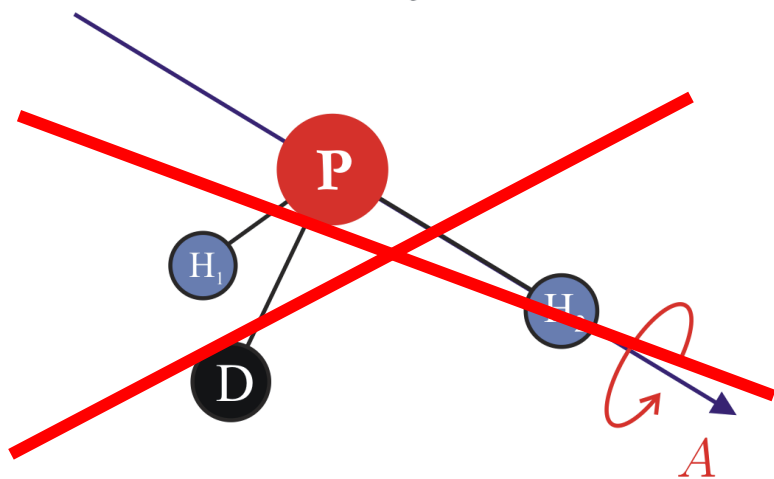
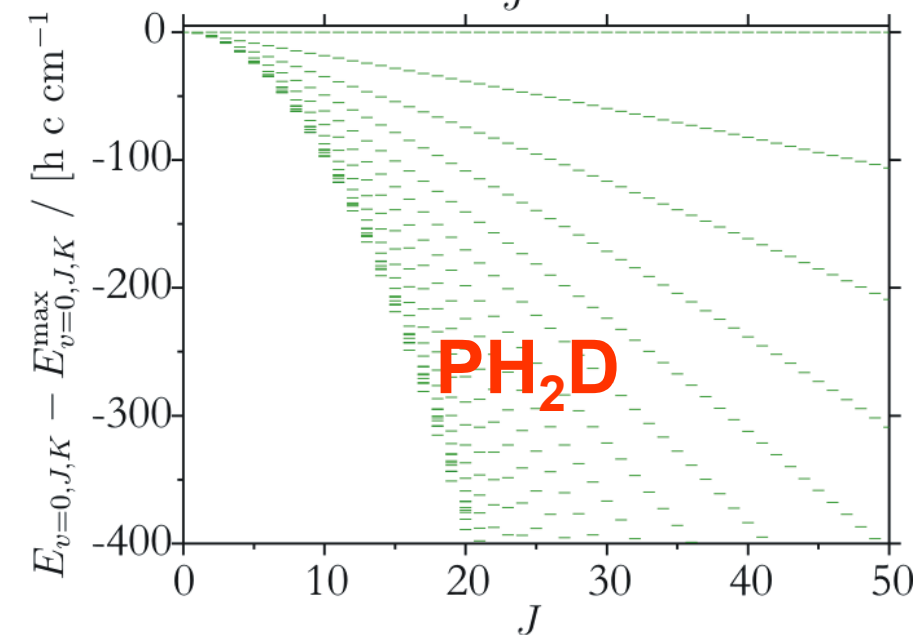
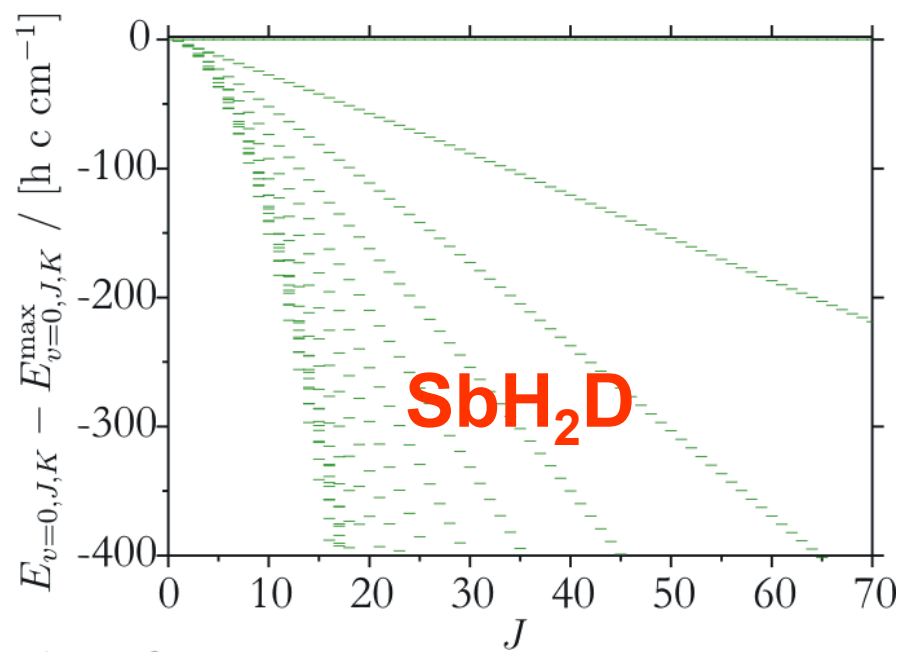
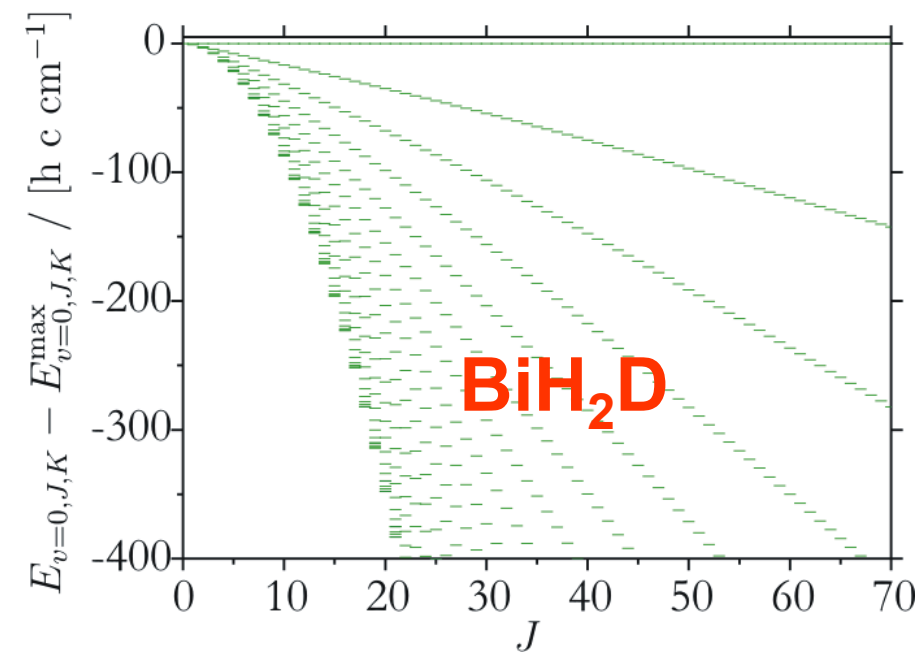


No cluster formation found for PH₂D

PH₂D

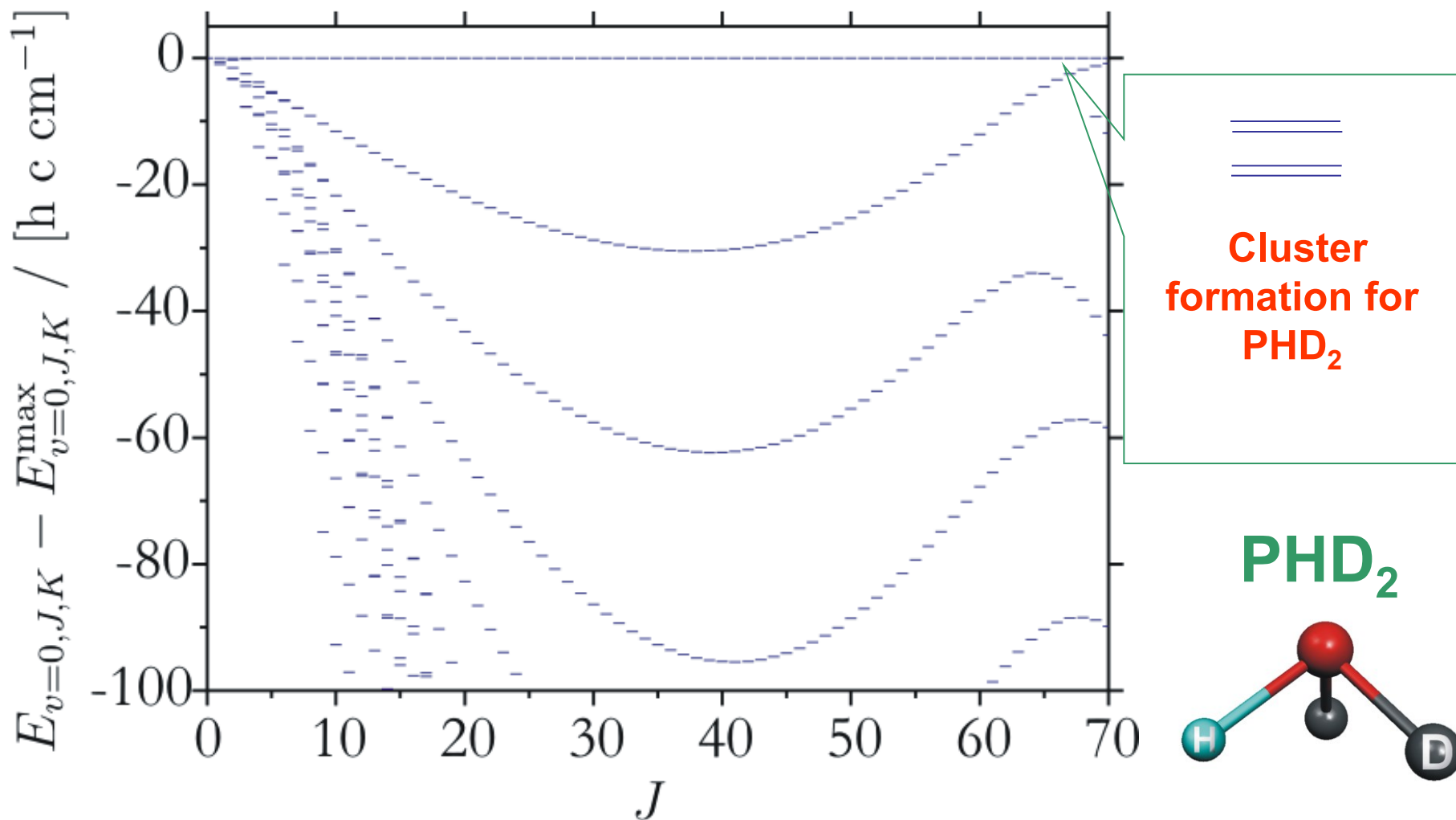


XH_2D : Cluster-free molecules



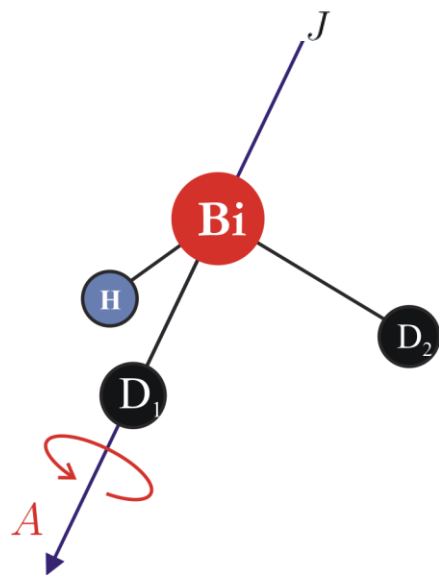
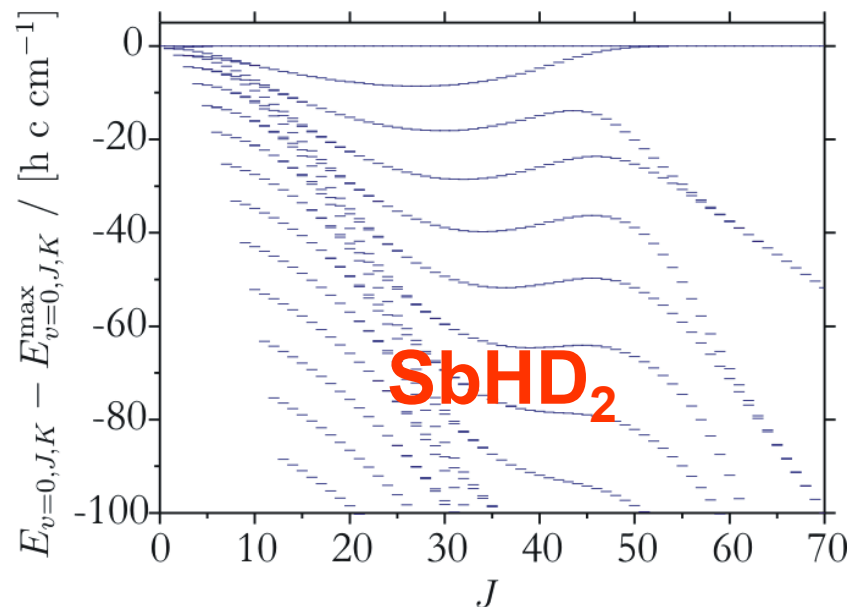
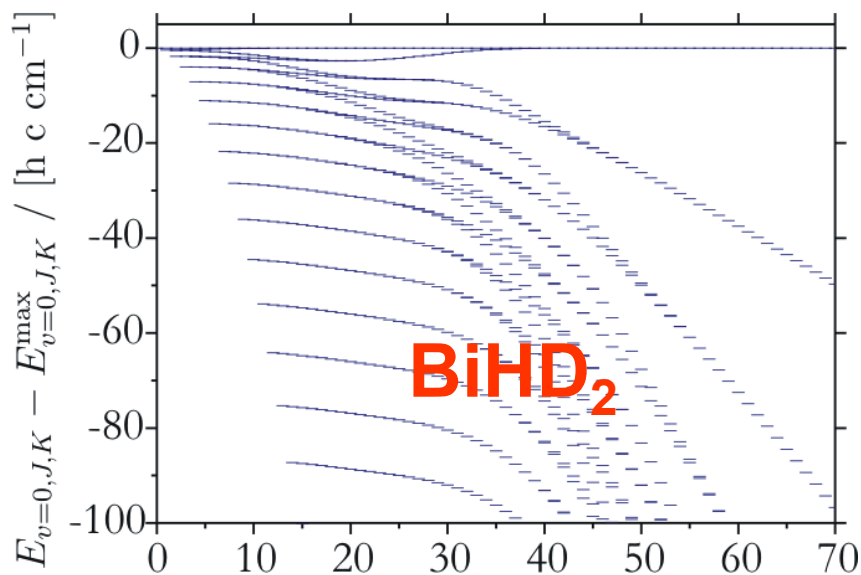
Reduced rotational term values

PHD₂ rotation energies: TROVE calculations

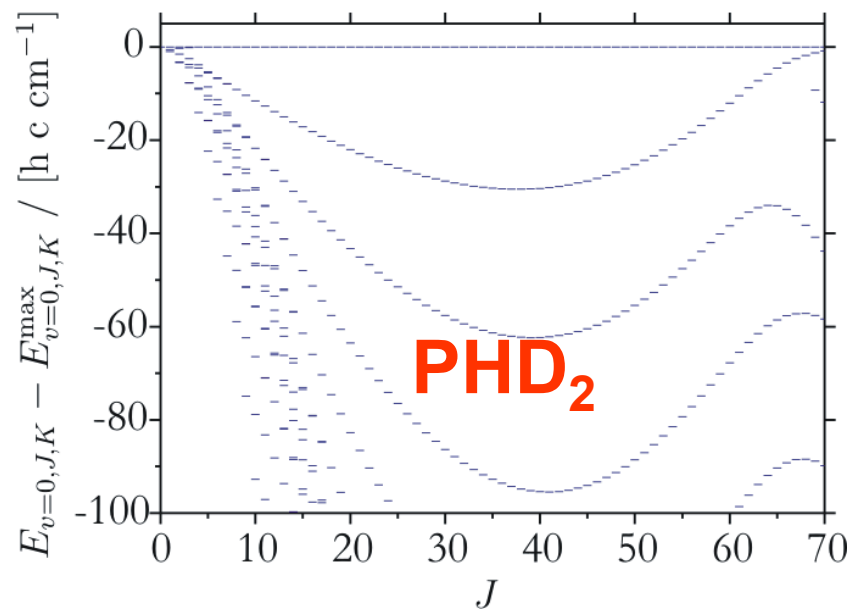


Reduced rotational term values in the vibrational ground state of PHD₂

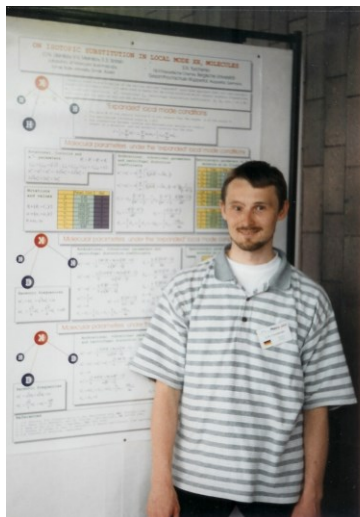
XHD₂: Molecules with rotational energy cluster formation



Reduced rotational term values



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The principal doer:

← **Sergei N. Yurchenko**, Wuppertal, Ottawa,
Mülheim, Dresden

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Serguei Patchkovskii, Ottawa

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